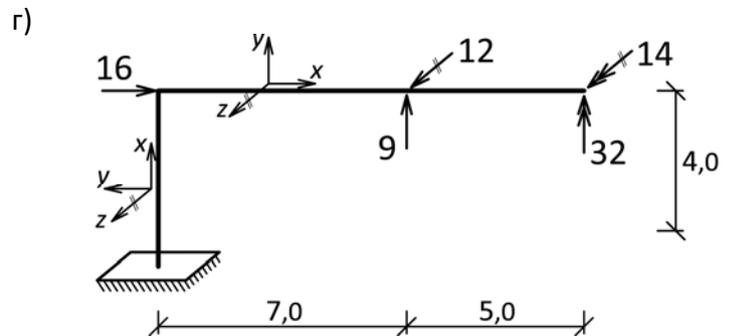
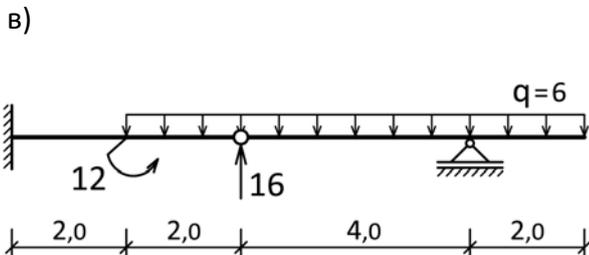
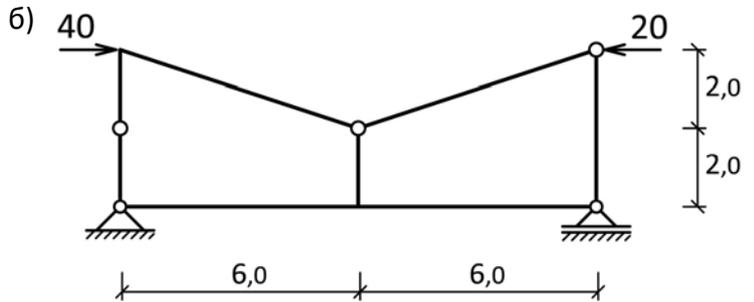
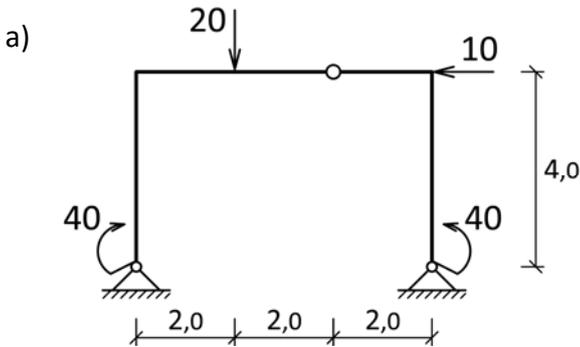


**ГРАЂЕВИНСКИ ФАКУЛТЕТ УНИВЕРЗИТЕТА У БЕОГРАДУ**  
 Усмени (теоријски) део испита из **ТЕХНИЧКЕ МЕХАНИКЕ 1**  
 (писмени део одржан 28.06.2018.)

**1. ЗАДАТАК** (условни 50 %)

Нацртати дијаграме сила у пресеку за приказане носаче.



**2. ЗАДАТАК** (28 %)

а) Приказати и укратко објаснити Aronhold-Kennedy-еву теорему.

б) Применом опште једначине статике одредити:

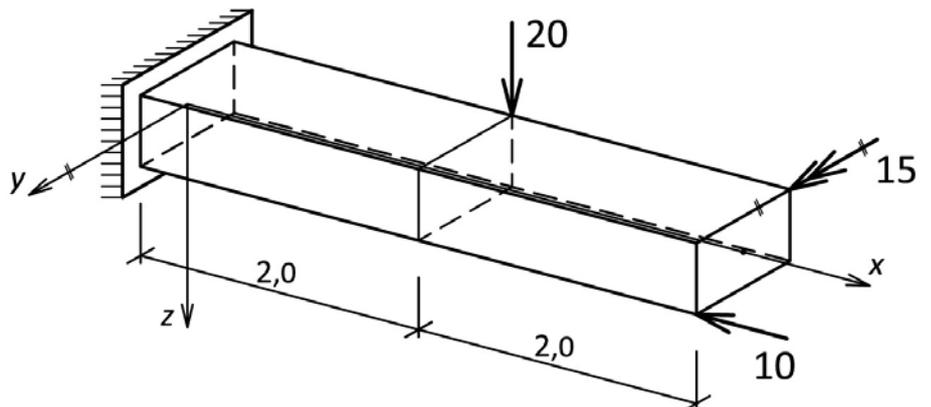
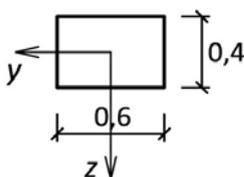
- \* хоризонталну реакцију веза у „десном“ непокретном ослонцу (задатак 1а),
- \* силу у „десном“ вертикалном простом штапу (задатак 1б),
- \* моменат у укљештењу (задатак 1в).

**3. ЗАДАТАК** (22 %)

а) Дефинисати моменат силе за осу и навести два става у вези са појмом момента силе за осу.

б) Извршити редукцију свог задатог оптерећења на осу посматраног конзолног штапа.

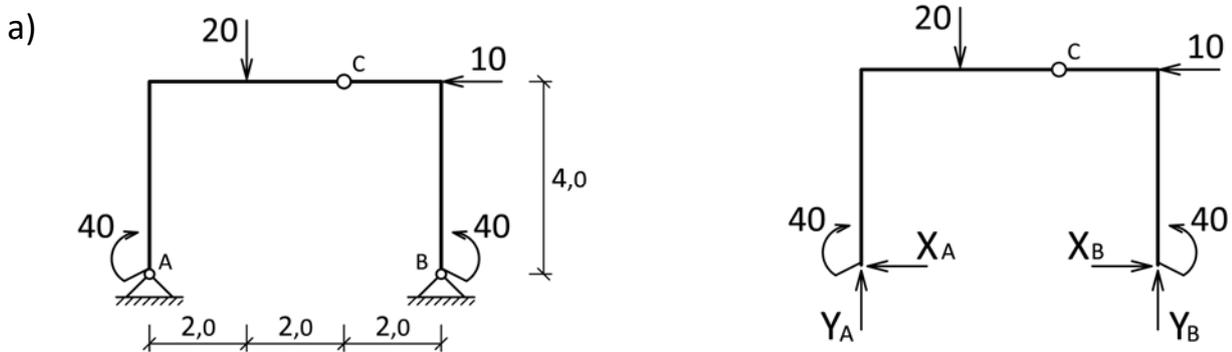
попечни пресек штапа



Напомена: У свим задацима димензије за дужине и силе су:  $m, N$

**- Р Е Ш Е Њ А -**

**1. ЗАДАТАК** (условни 50 %)

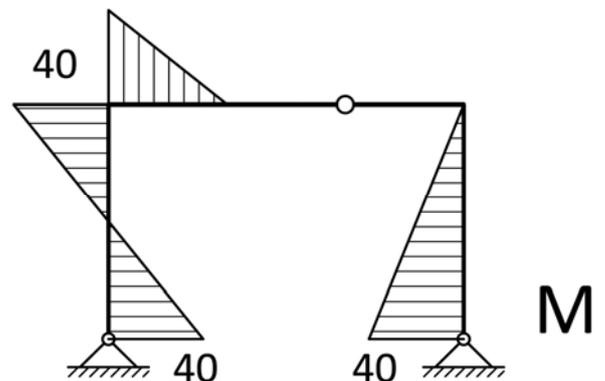
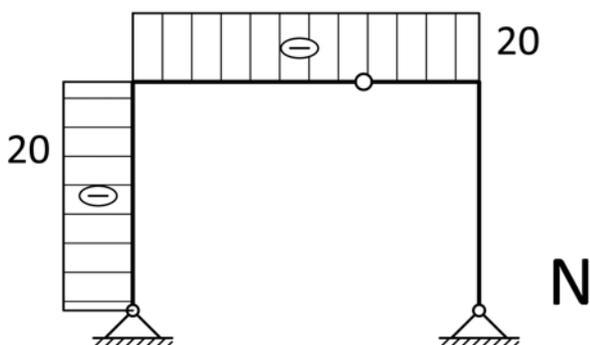
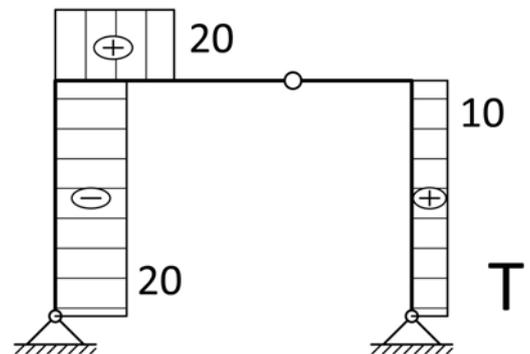
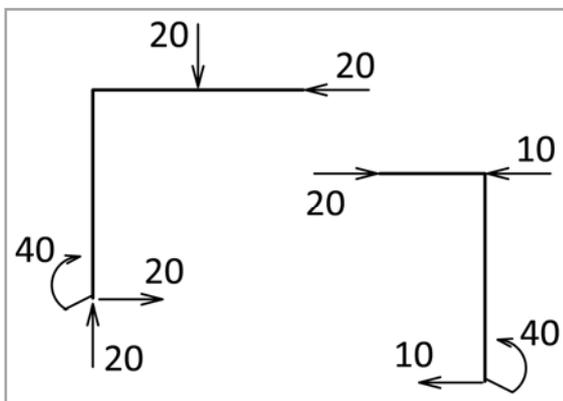


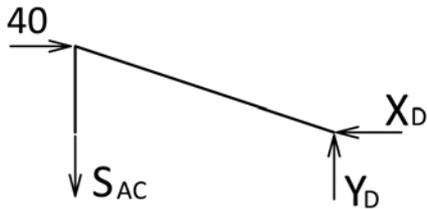
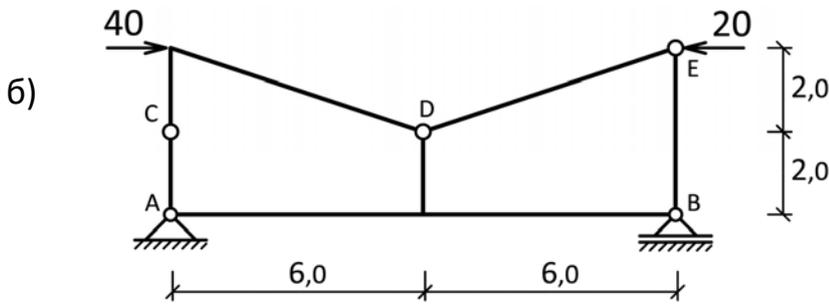
$$\sum M_A = 0 : Y_B \cdot 6 + 10 \cdot 4 - 20 \cdot 2 + 30 - 40 = 0 \rightarrow \underline{Y_B = 0}$$

$$\sum F_Y = 0 : Y_A + Y_B - 20 = 0 \rightarrow \underline{Y_A = 20}$$

$$\sum M_{C, дес} = 0 : X_B \cdot 4 + Y_B \cdot 2 + 40 = 0 \rightarrow \underline{X_B = -10}$$

$$\sum F_X = 0 : -X_A + X_B - 10 = 0 \rightarrow \underline{X_A = -20}$$

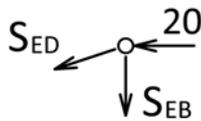




$$\sum F_x = 0 : -X_D + 40 = 0 \rightarrow \underline{X_D = 40}$$

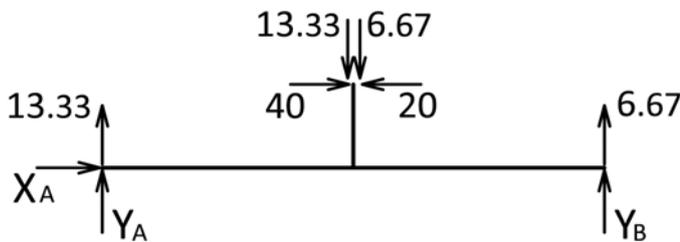
$$\sum M_D = 0 : S_{AC} \cdot 6 - 40 \cdot 2 = 0 \rightarrow \underline{S_{AC} = 13.33}$$

$$\sum F_y = 0 : Y_D - S_{AC} = 0 \rightarrow \underline{Y_D = 13.33}$$



$$\sum F_x = 0 : -0.949 \cdot S_{ED} - 20 = 0 \rightarrow \underline{S_{ED} = -21.08}$$

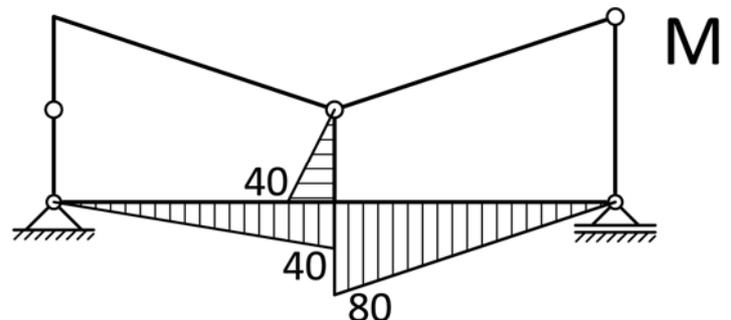
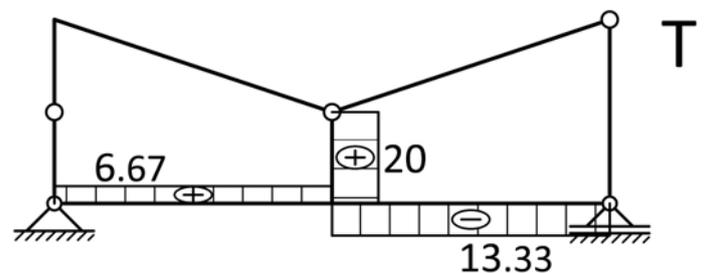
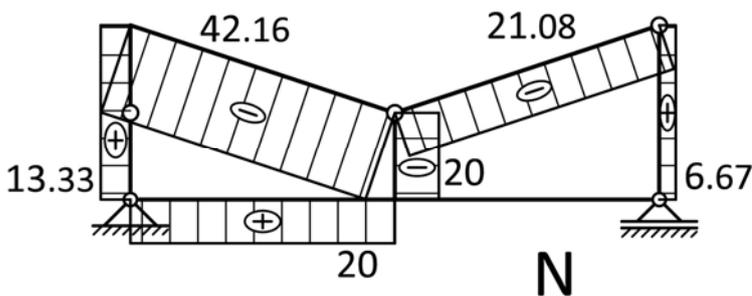
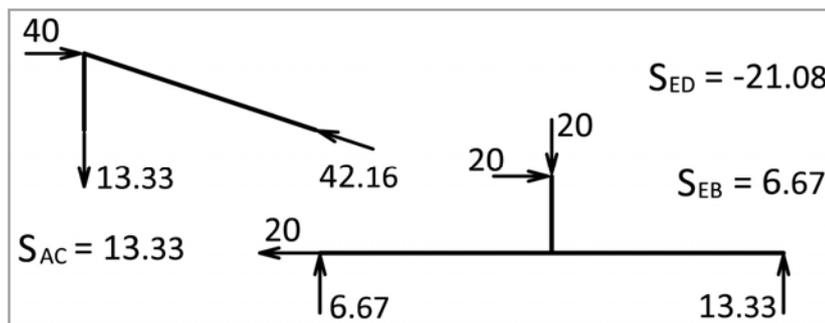
$$\sum F_y = 0 : -0.316 \cdot S_{ED} - S_{EB} = 0 \rightarrow \underline{S_{EB} = 6.67}$$



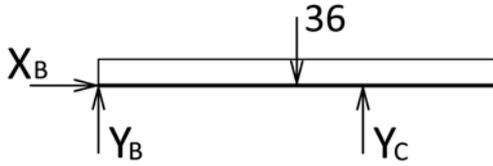
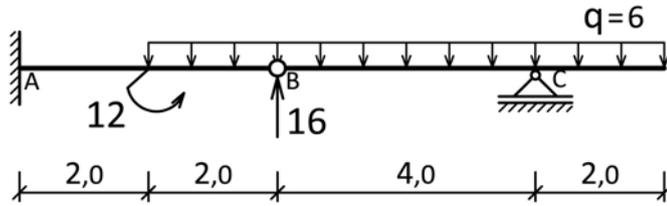
$$\sum F_x = 0 : X_A + 40 - 20 = 0 \rightarrow \underline{X_A = -20}$$

$$\sum M_A = 0 : Y_B \cdot 12 + 6.67 \cdot 12 - 20 \cdot 6 - 20 \cdot 2 = 0 \rightarrow \underline{Y_B = 6.67}$$

$$\sum F_y = 0 : Y_A + Y_B + 13.33 + 6.67 - 20 = 0 \rightarrow \underline{Y_A = -6.67}$$



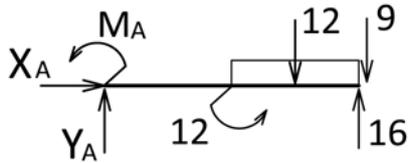
B)



$$\sum F_x = 0 : \rightarrow X_B = 0$$

$$\sum M_B = 0 : Y_C \cdot 4 - 36 \cdot 3 = 0 \rightarrow Y_C = 27$$

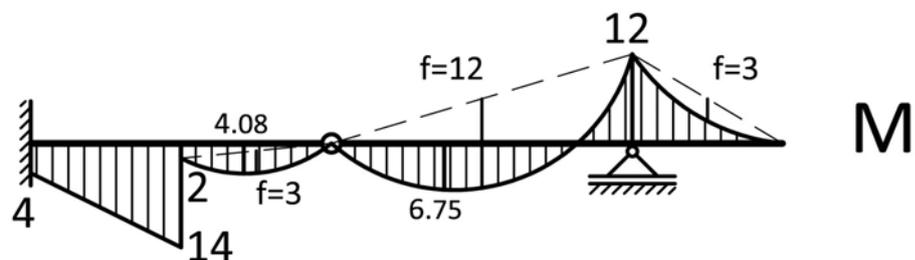
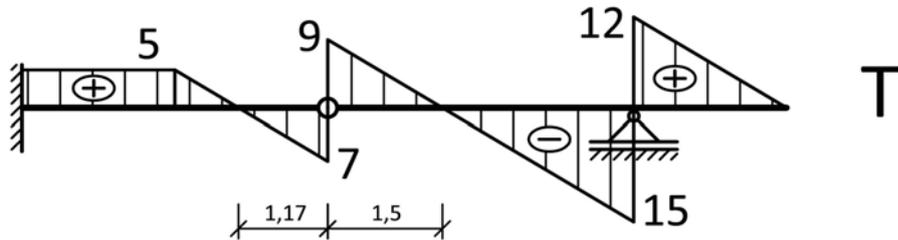
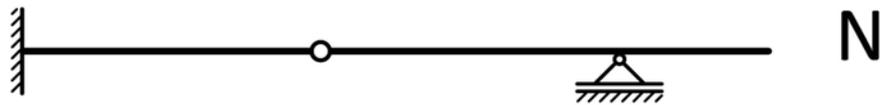
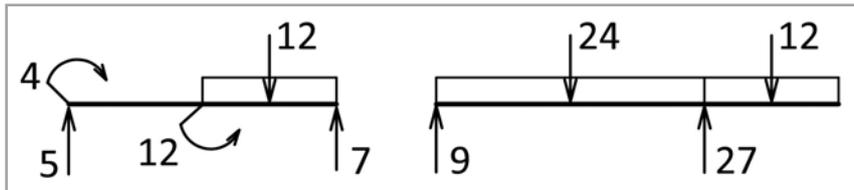
$$\sum F_y = 0 : Y_B + Y_C - 36 = 0 \rightarrow Y_B = 9$$



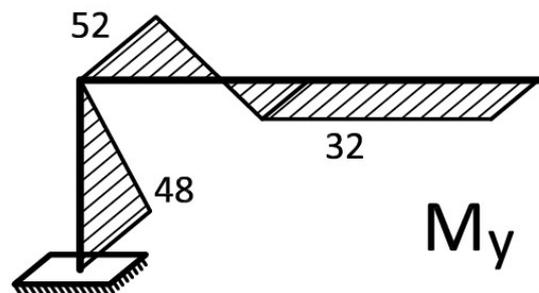
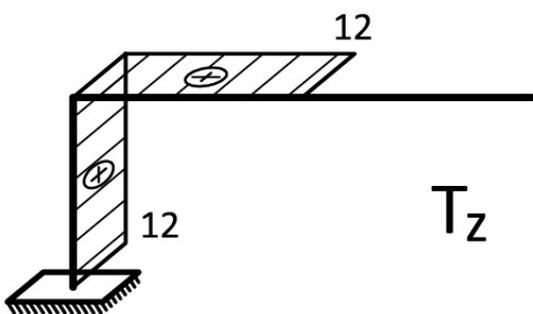
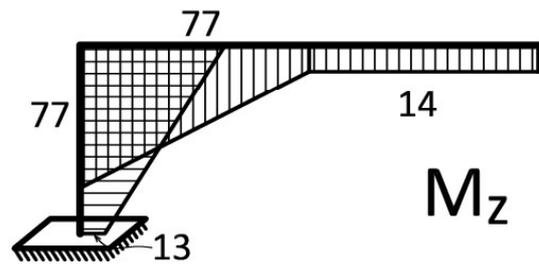
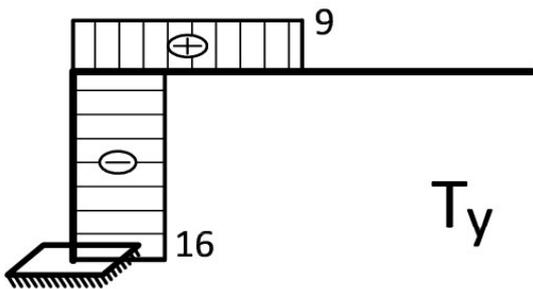
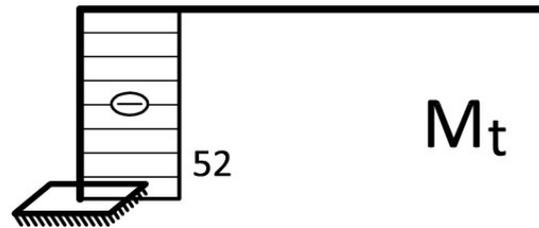
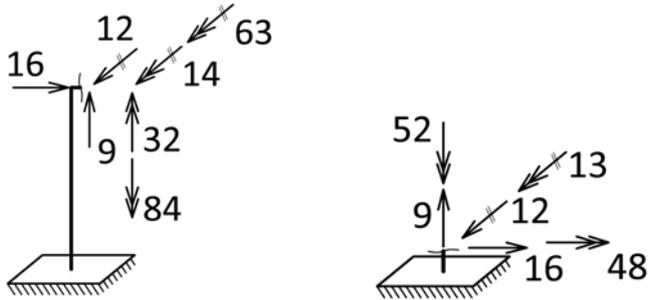
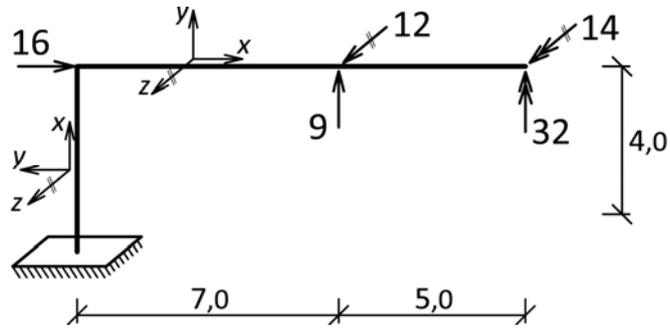
$$\sum F_x = 0 : \rightarrow X_A = 0$$

$$\sum F_y = 0 : Y_A - 12 + 16 - 9 = 0 \rightarrow Y_A = 5$$

$$\sum M_A = 0 : M_A + (16-9) \cdot 4 - 12 \cdot 3 + 12 = 0 \rightarrow M_A = -4$$

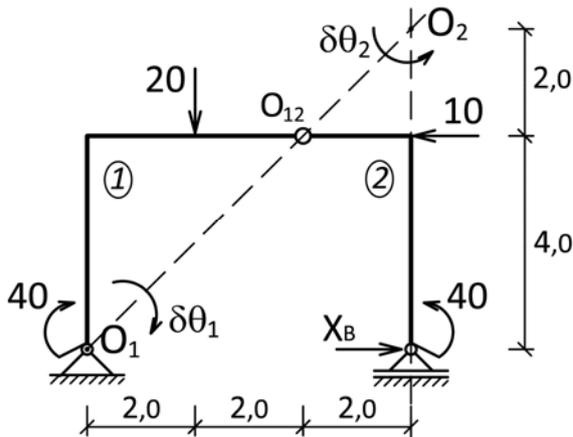


r)



**2. ЗАДАТАК** (28 %)

б)  $X_B = ?$  (зад. 1а)

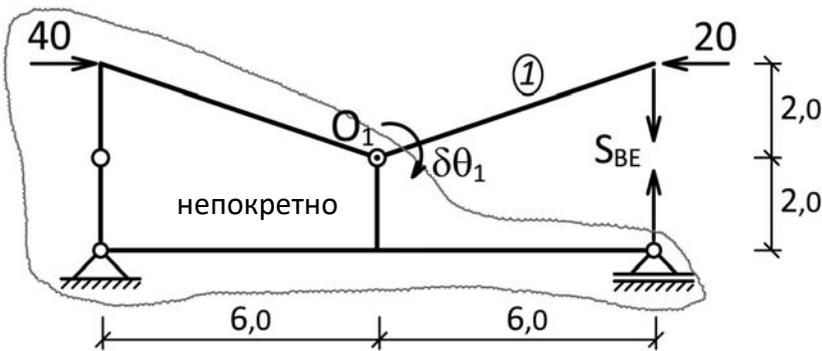


$$\delta r_{O_{12},y} = \delta \theta_1 \cdot 4 = \delta \theta_2 \cdot 2 \rightarrow \delta \theta_1 = 0.5 \cdot \delta \theta_2$$

$$\delta A = X_B \cdot (6 \cdot \delta \theta_2) - 10 \cdot (2 \cdot \delta \theta_2) + 20 \cdot (2 \cdot \delta \theta_1) + 40 \cdot \delta \theta_1 + 40 \cdot \delta \theta_2 = 0$$

$$6 \cdot X_B \cdot \delta \theta_2 + 60 \cdot \delta \theta_2 = 0 \rightarrow \underline{X_B = -10.0}$$

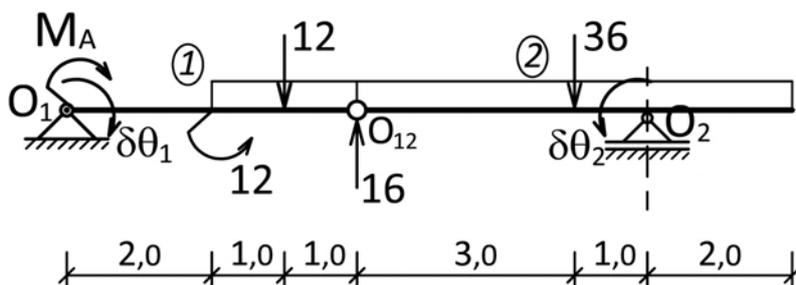
$S_{BE} = ?$  (зад. 1б)



$$\delta A = S_{BE} \cdot (6 \cdot \delta \theta_1) - 20 \cdot (2 \cdot \delta \theta_1) = 0$$

$$\rightarrow \underline{S_{BE} = 6.67}$$

$M_A = ?$  (зад. 1в)



$$\delta r_{O_{12},y} = \delta \theta_1 \cdot 4 = \delta \theta_2 \cdot 4$$

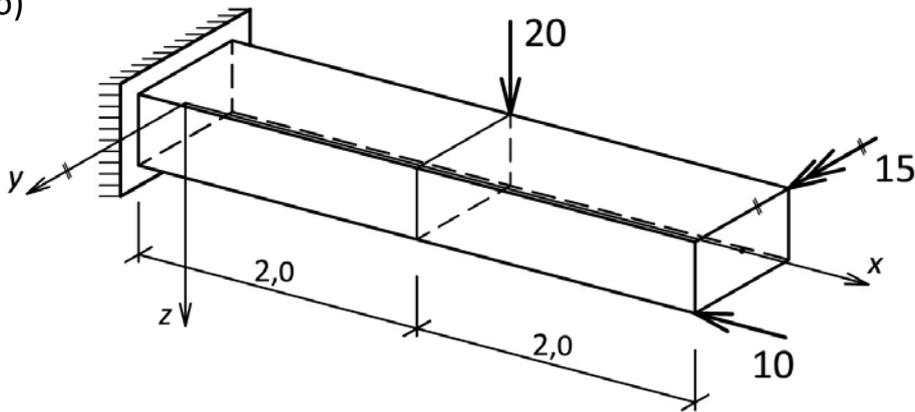
$$\rightarrow \delta \theta_1 = \delta \theta_2$$

$$\delta A = M_A \cdot \delta \theta_1 - 12 \cdot \delta \theta_1 + 12 \cdot (3 \cdot \delta \theta_1) - 16 \cdot (4 \cdot \delta \theta_1) + 36 \cdot (1 \cdot \delta \theta_1) = 0$$

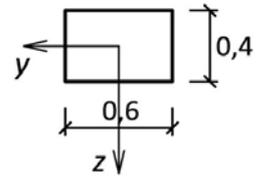
$$M_A \cdot \delta \theta_1 - 4 \cdot \delta \theta_1 = 0 \rightarrow \underline{M_A = 4}$$

### 3. ЗАДАТАК (22 %)

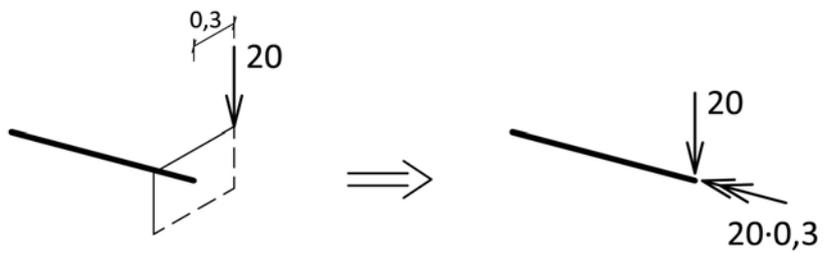
б)



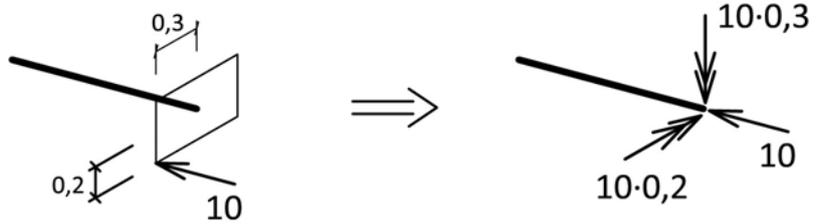
попречни пресек штапа



- редуција силе  $F_z = 20$   
на осу штапа



- редуција силе  $F_x = 10$   
на осу штапа



Силе редуковане на осу штапа

